



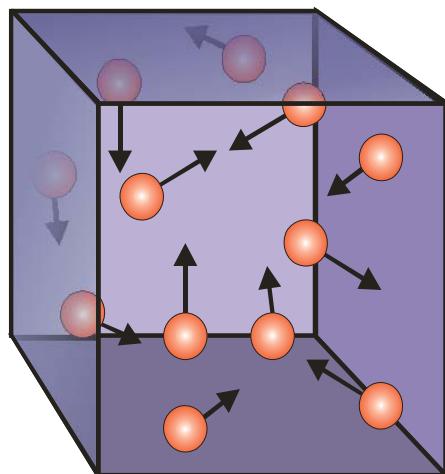
# Quanteneffekte in Halbleiter nanostrukturen

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Gottfried Wilhelm Leibniz Universität Hannover  
Germany

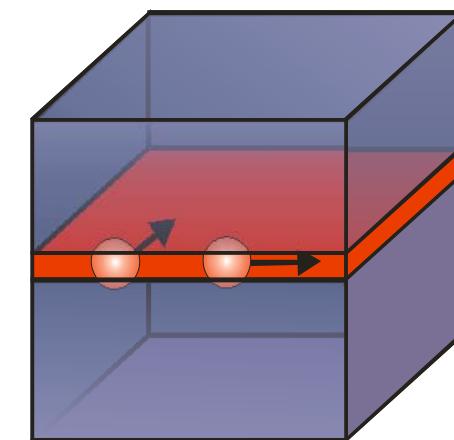
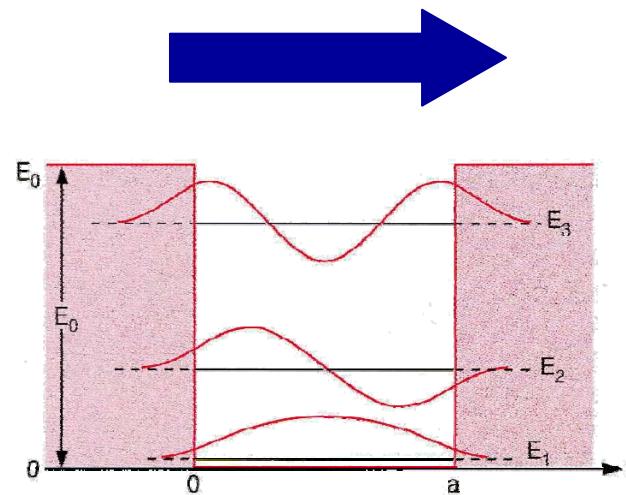
# Quantum Mechanics: Low-Dimensional Systems

3d



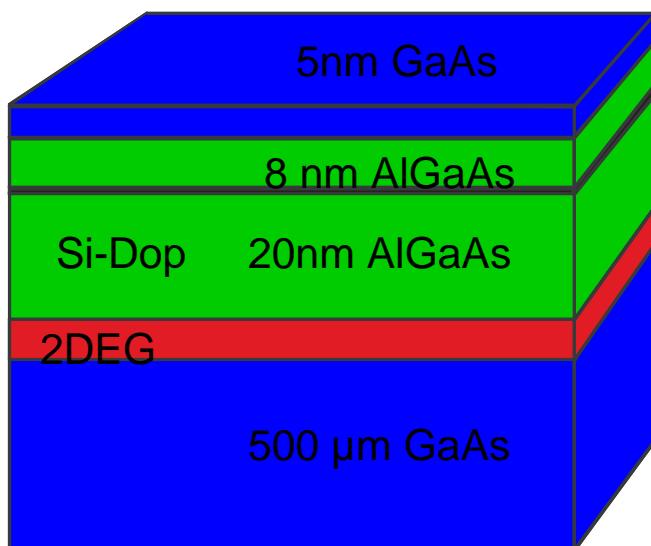
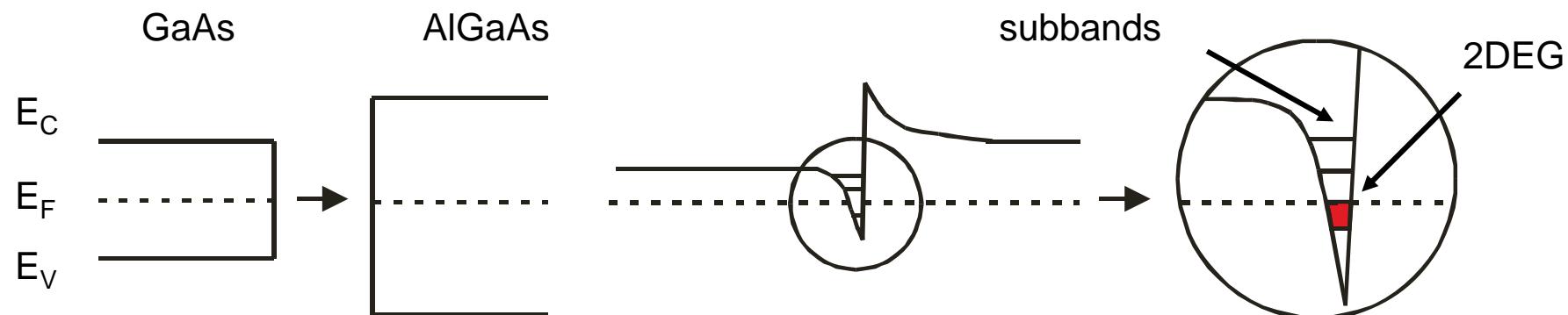
2d

quantum size effect



particles have signatures of waves

# 2D in Semiconducting Heterostructures



2d

- **band-edge discontinuity produces triangular well**  $\rightarrow$  **2DEG**

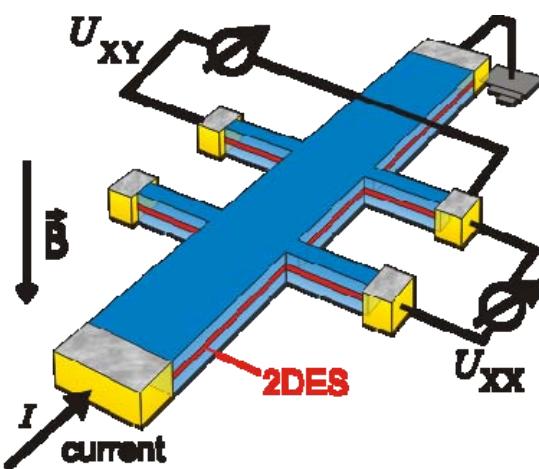
made by  
molecular beam epitaxy

used in

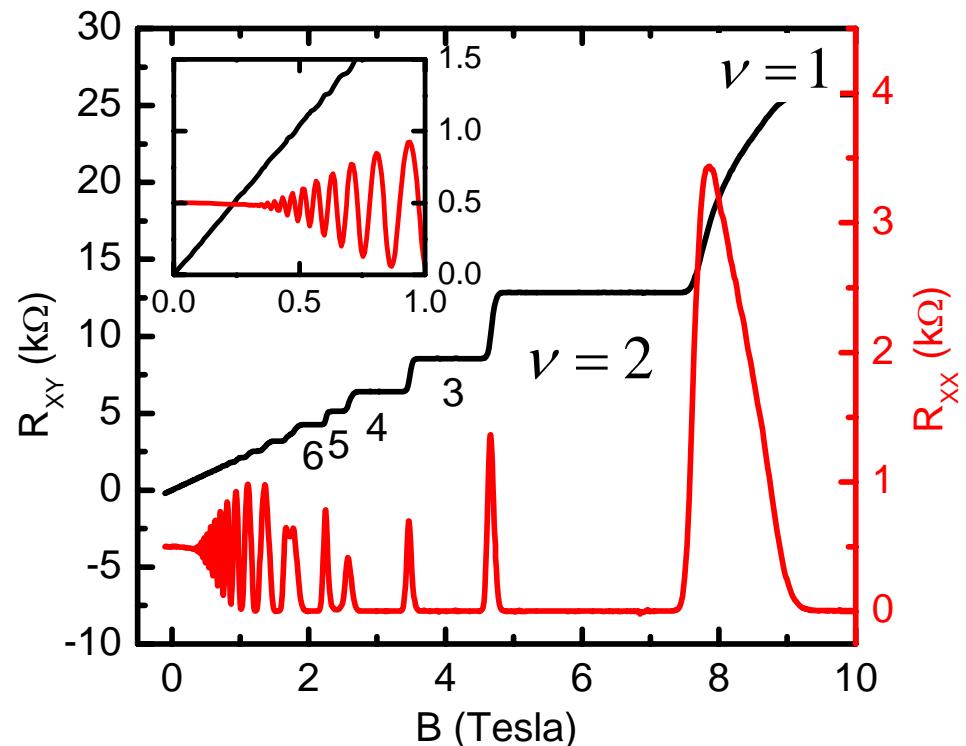


# 2d Physics: Quantum Hall Effect

DFG Priority Program: 2000 - 2006

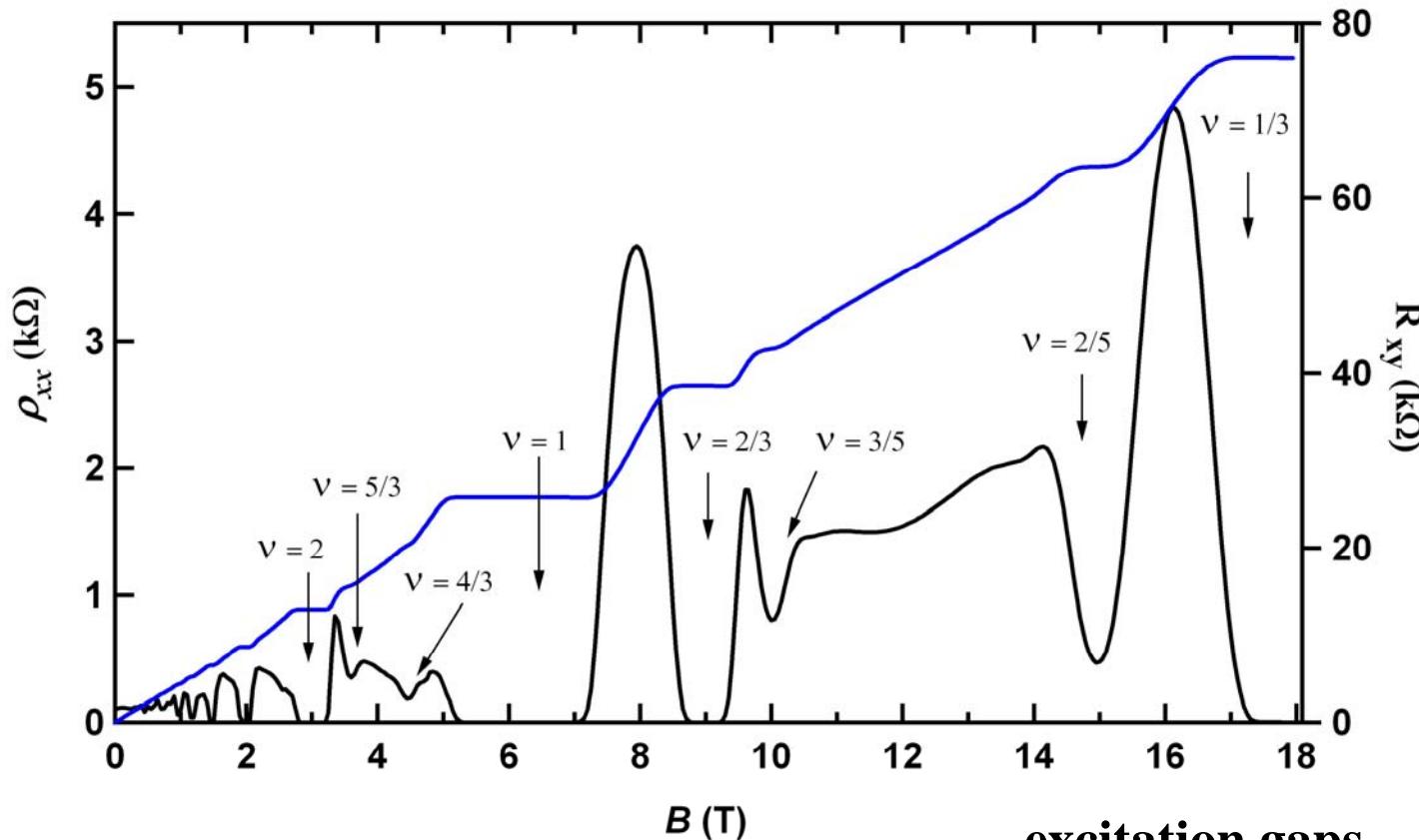


$$R_{XY} = \frac{U_{XY}}{I} = \frac{h}{ve^2} = \frac{1}{\nu} 25812,807 \Omega$$



- Phys. Rev. Lett. 93, 196801 (2004)  
Phys. Rev. Lett. 89, 276801 (2002)  
Phys. Rev. Lett. 88, 036802 (2002)  
Phys. Rev. Lett. 86, 5124 (2001)

# Fractional Quantum Hall Effect



cond-mat/0607167

Phys. Rev. B 74, 165325 (2006)

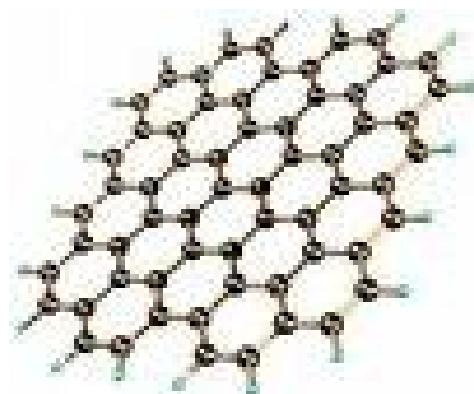
Phys. Rev. B 74, 195324 (2006)

Phys. Rev. Lett. 92, 156401 (2004)

Phys. Rev. Lett. 93, 026801 (2004)

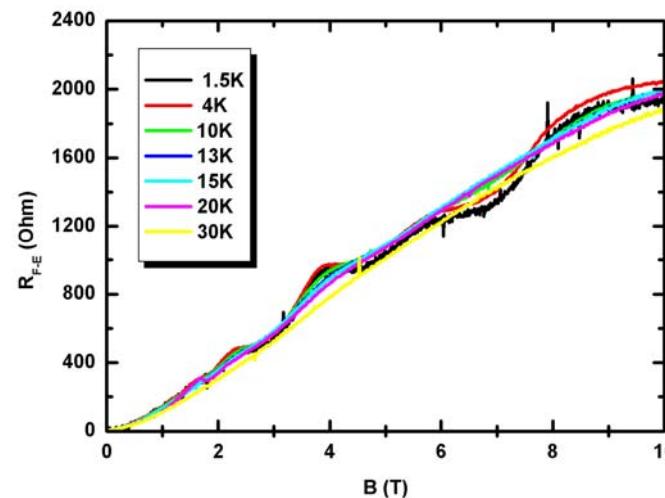
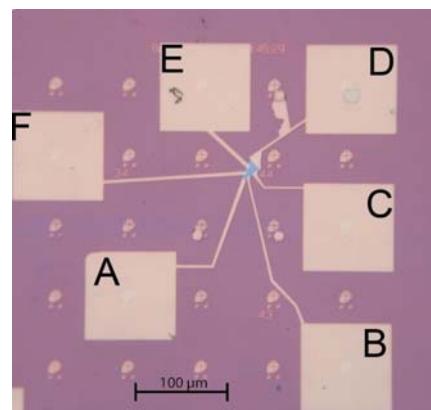
excitation gaps  
effects of spin,  
specific heat,  
electrons versus holes

# Quantum Hall Effect at Room Temperature Novel Material: Graphene



Novoselov et al., Science 315 (2007)

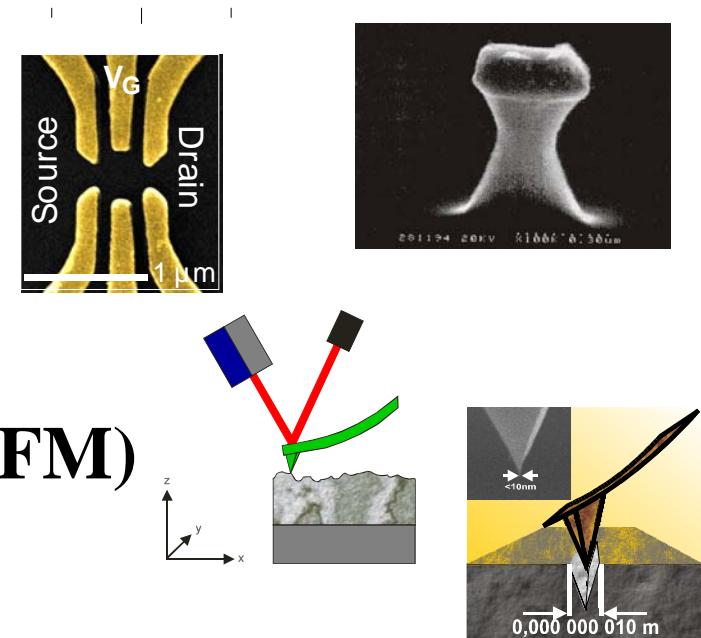
our measurements:  
not yet as good



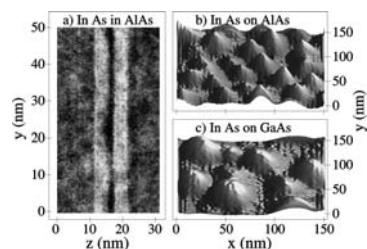


# Low-Dimensional Structures: 1d, 0d

- **lithography**
  1. optical lithography
  2. electron beam lithography
  3. direct writing with atomic force microscope (AFM)



- **self-organized growth**  
**quantum dots (InAs, Si, Ge)**

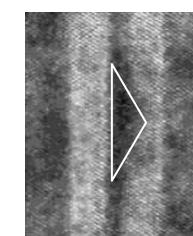


lattice mismatch between InAs

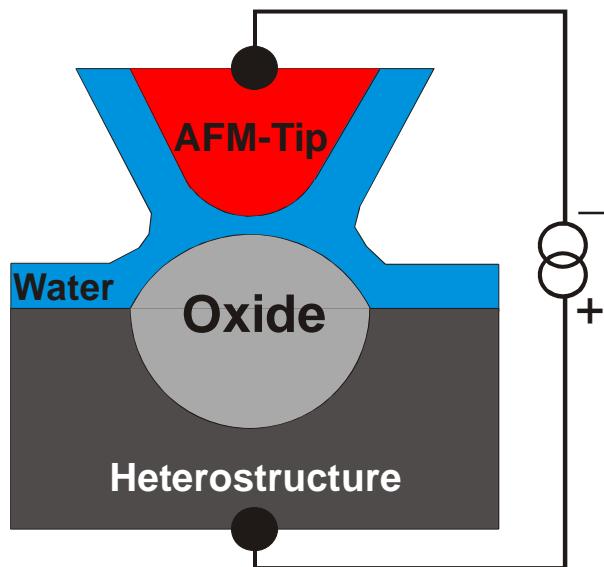
and AlAs (GaAs): 7%

Stranski Krastanov growth

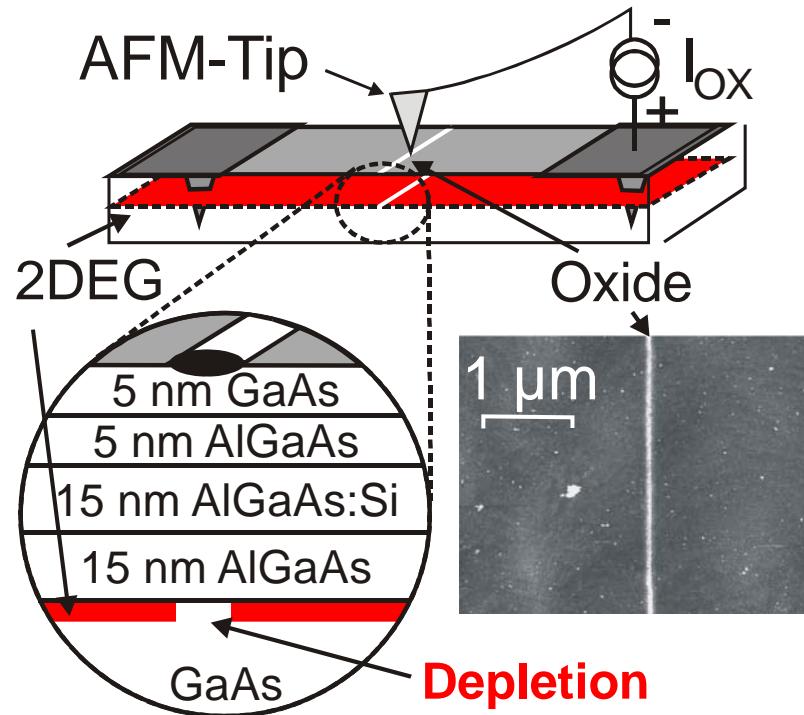
Appl. Phys. Lett. 82, 1209 (2003)



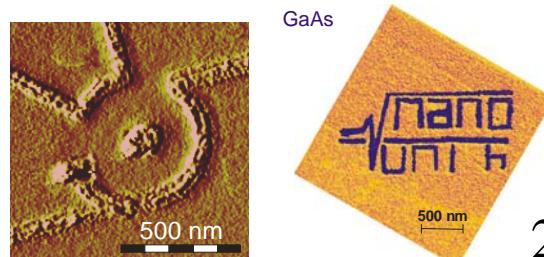
# Local Oxidation with AFM



Appl. Phys. Lett. 76, 457 (2000)



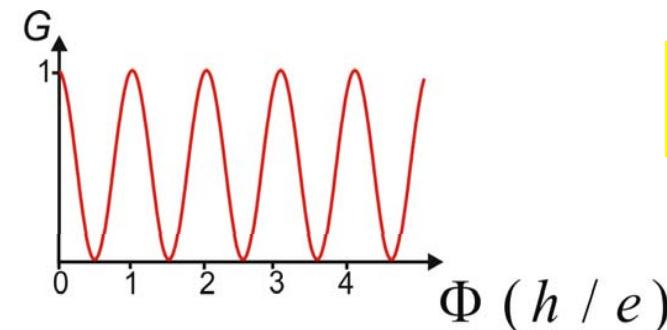
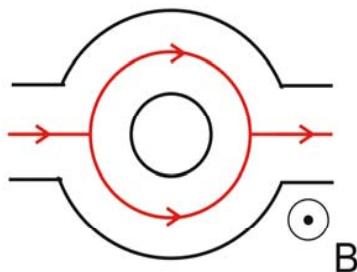
Ishii, Matsumoto (1995)



chemistry:

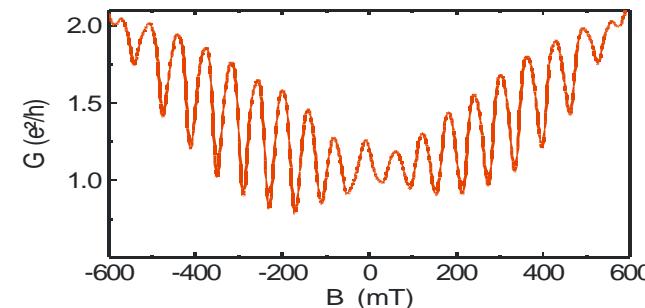
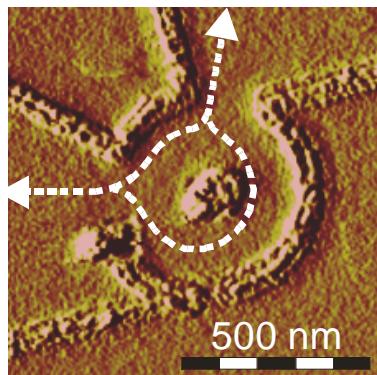


# Interference Effects in Quantum Rings



$$G \propto \cos(2\pi \Phi / \Phi_0)$$

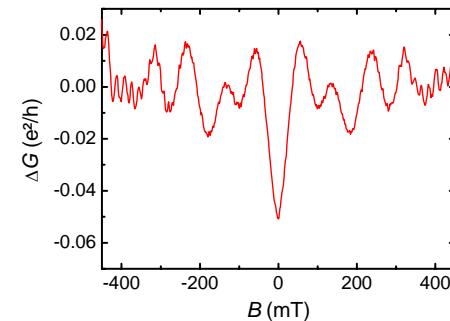
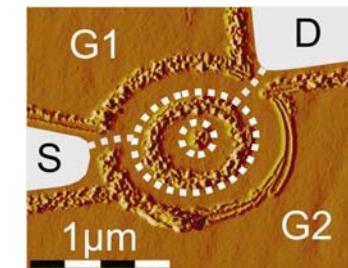
flux quant.:  $\Phi_0 = h/e$   
Aharanov-Bohm effect



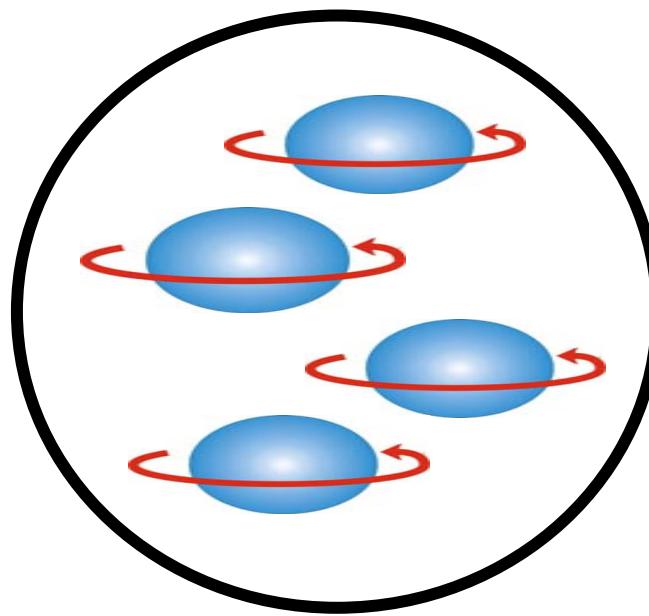
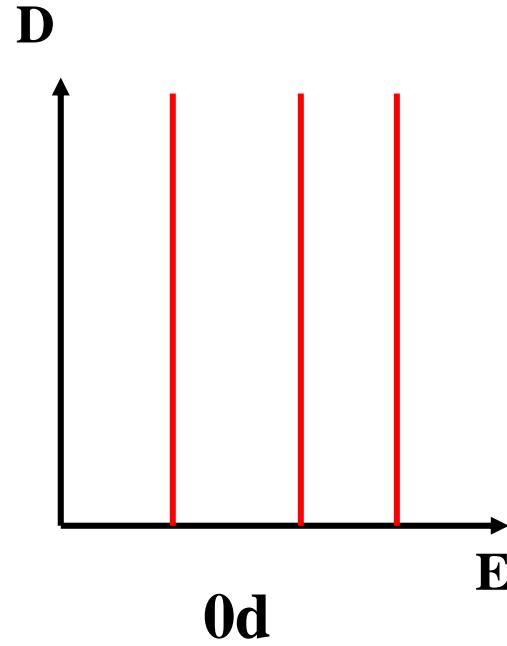
up to 50% modulation of  
the conduct. periodicity  
58mT: R=150nm

Phys. Rev. Lett. 90, 196601 (2003)

2 rings:

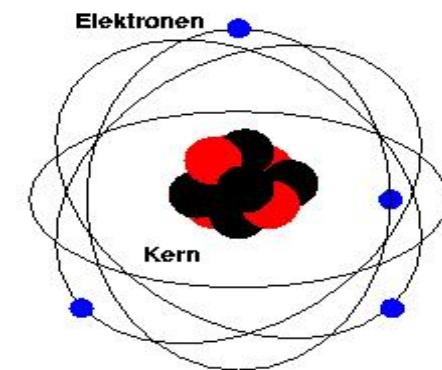


# Quantum Dot: quasi-zerodimensional system in a semiconductor



charge, spin,  
interaction effects,  
quantum information processing

artificial atom?!

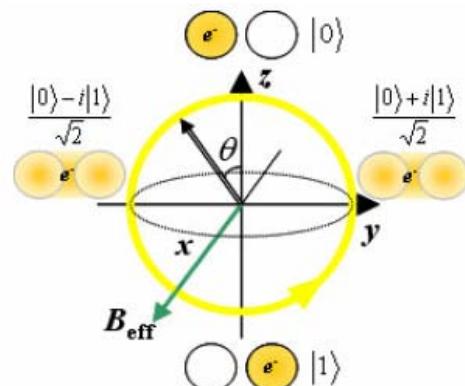


Bohr radius

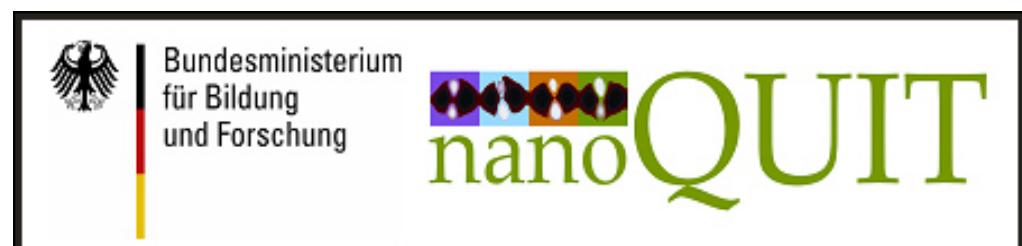
$$a_B = \frac{4\pi\hbar^2\epsilon\epsilon_0}{me^2}$$

# Quantum Information Processing: Calculating with Quantum Mechanics

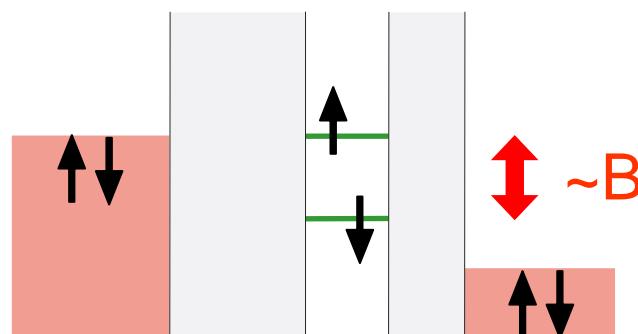
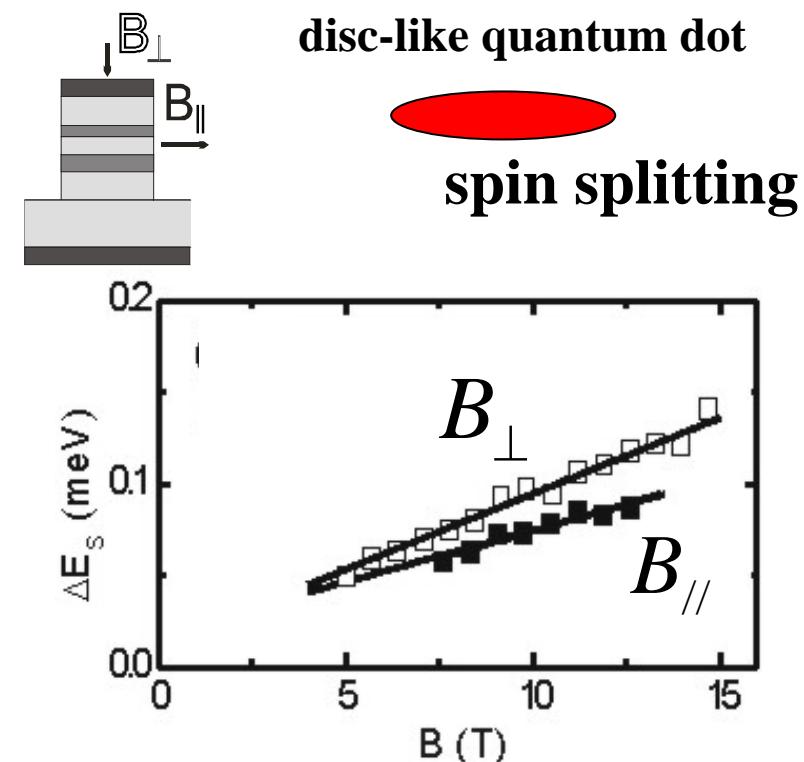
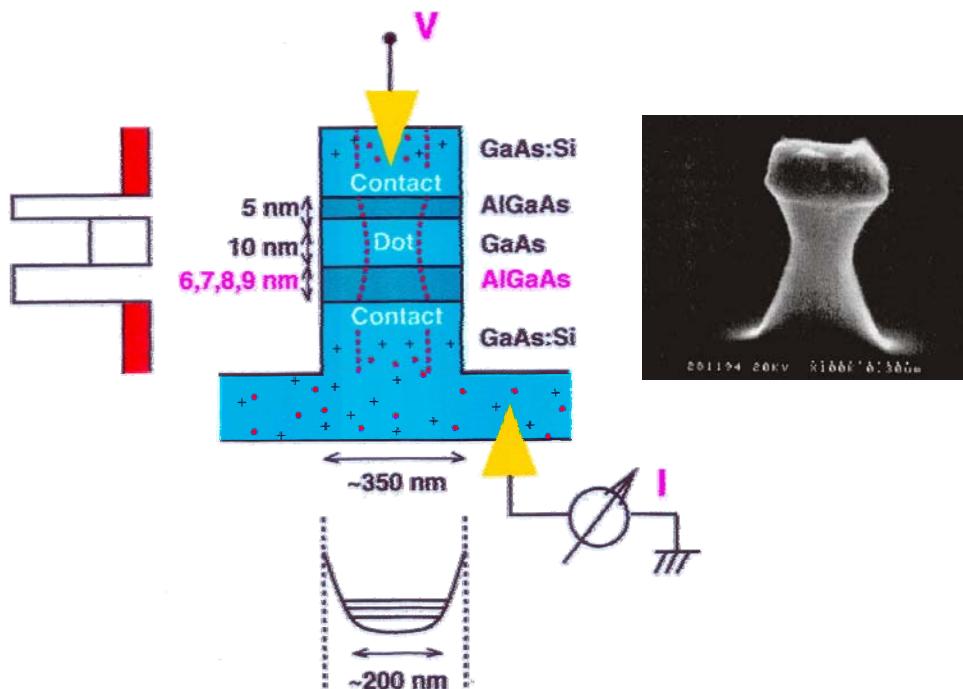
$$| \uparrow \rangle + | \downarrow \rangle$$



two-level systems in  
quantum dots:  
• charge  
• spin



# Spin Effects in Single Dots



differences due to spin-orbit effects

Phys. Rev. Lett. 94, 226404 (2005)

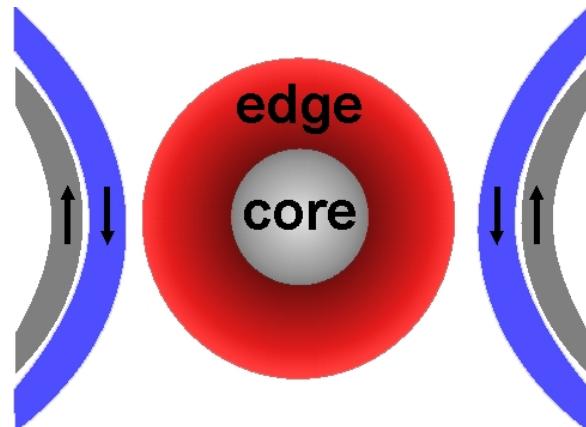
extreme anisotropy: holes in SiGe/Ge structure

$g=6.2 \rightarrow 0$

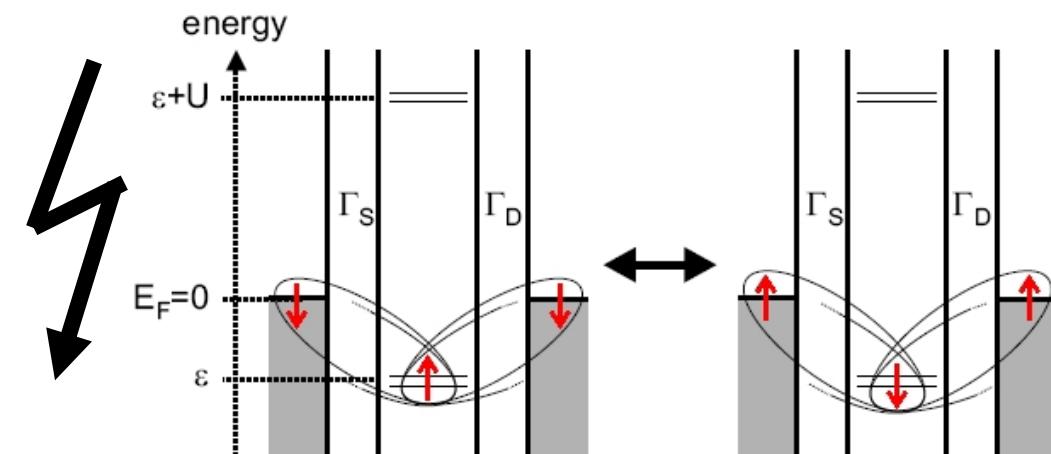
Phys. Rev. Lett. 96, 086403 (2006)

# Interaction Effects in Single Dots: Kondo Effect versus Spin Blockade

spin blockade



Kondo effect



spin-polarized leads necessary

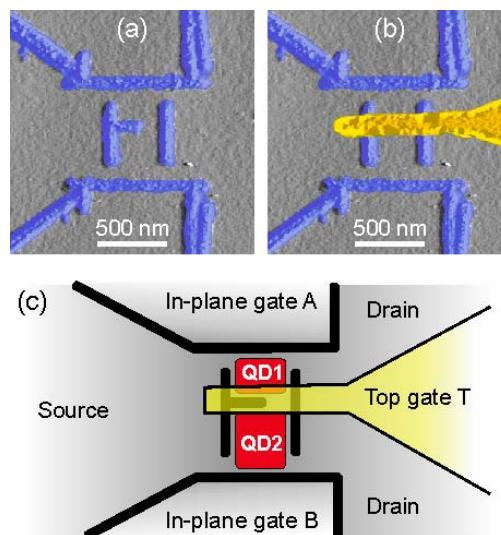
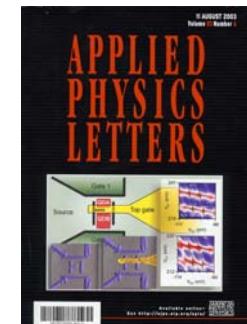
both spins in the leads necessary

→ spin structure of many-electrons quantum dots

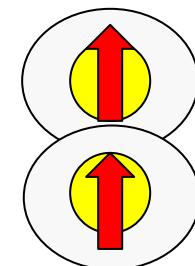
Phys. Rev. Lett. 96, 046802 (2006)

Phys. Rev. Lett. 96, 176801 (2006)

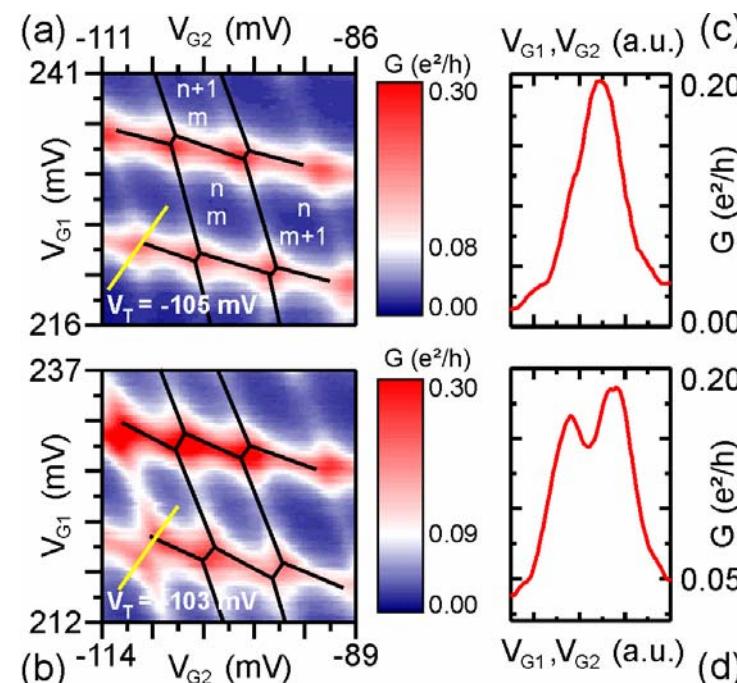
# Coupling between Quantum Dots: Artificial Molecule



Appl. Phys. Lett. 83, 1163 (2003)  
Appl. Phys. Lett. 85, 806 (2004)



**coupled quantum dots:  
building blocks of quantum comp.**



**weak  
coupling**

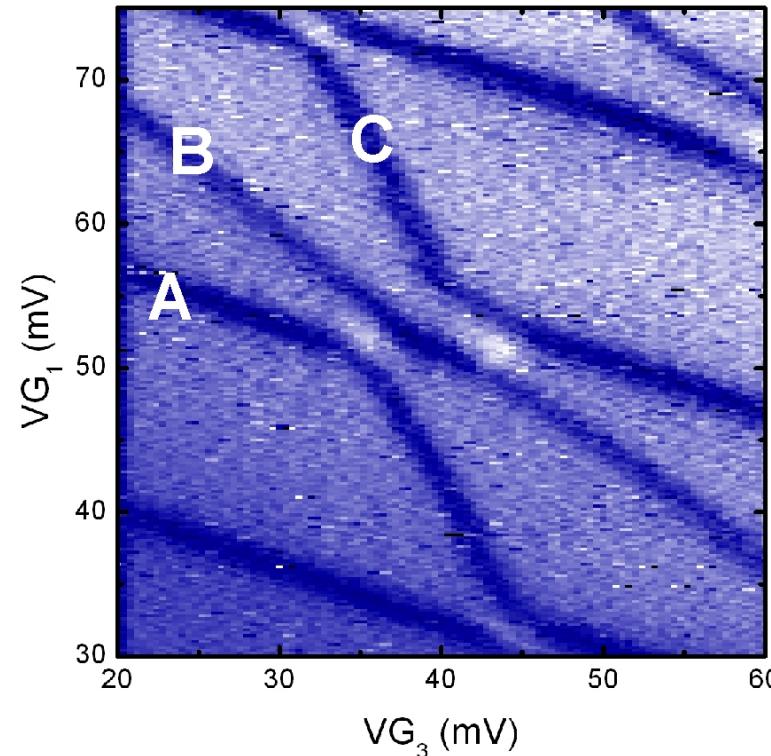
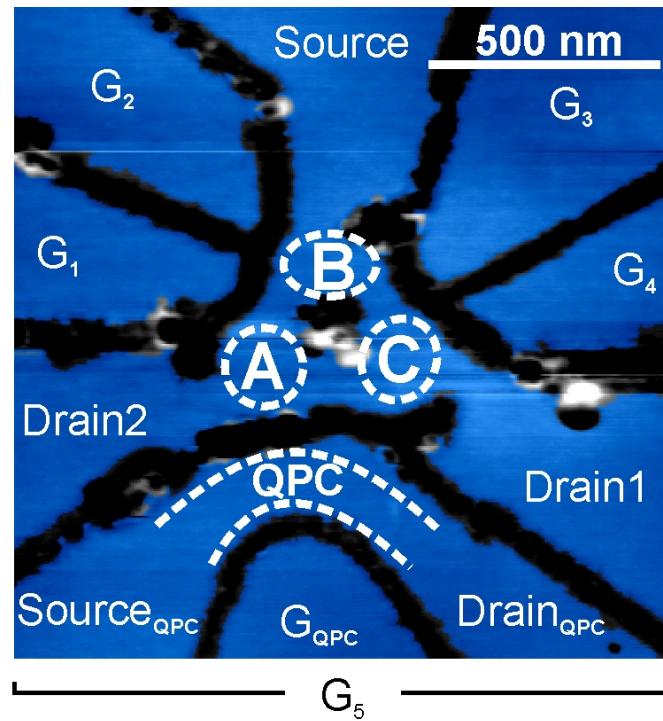
**strong  
coupling**

Phys. Rev. Lett. 96, 246803 (2006)

Phys. Rev. Lett. 80, 4032 (1998)

Phys. Rev. Lett. 81, 689 (1998)

# Triple Quantum Dot

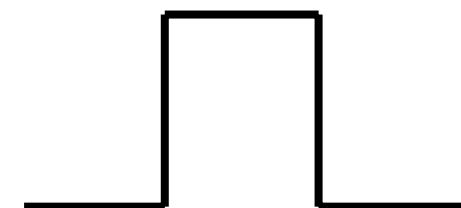
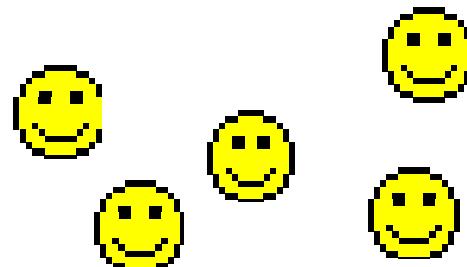


- triple quantum dot made with local anodic oxidation
- charge detection with quantum point contact

# Shot Noise

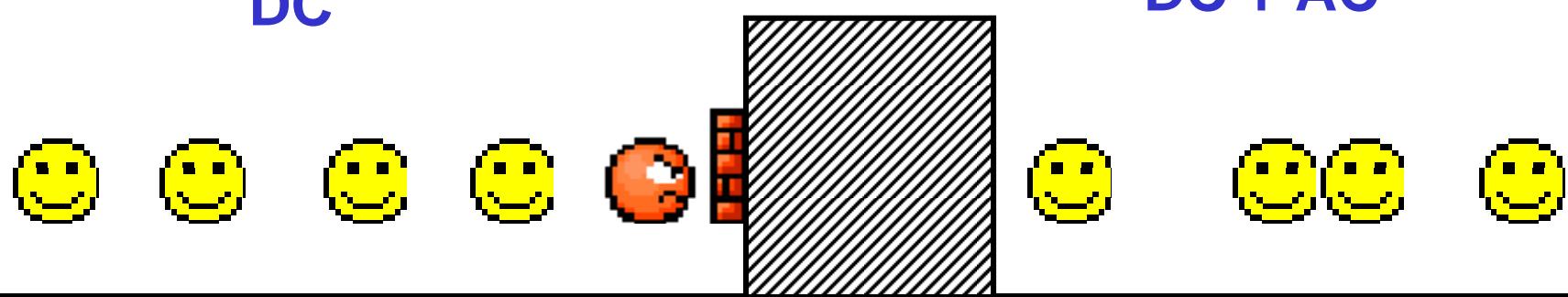
- electrical current

barrier

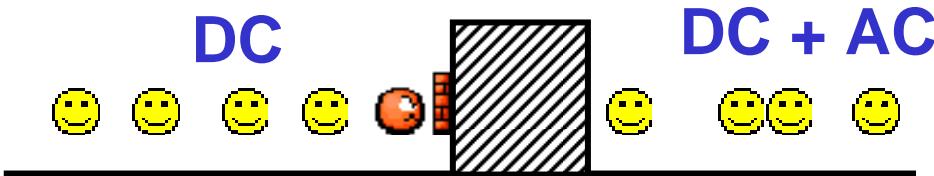


DC

DC + AC



# Shot Noise Suppression



$$S_{\text{Poisson}} = 2eI \quad (\text{single barrier})$$

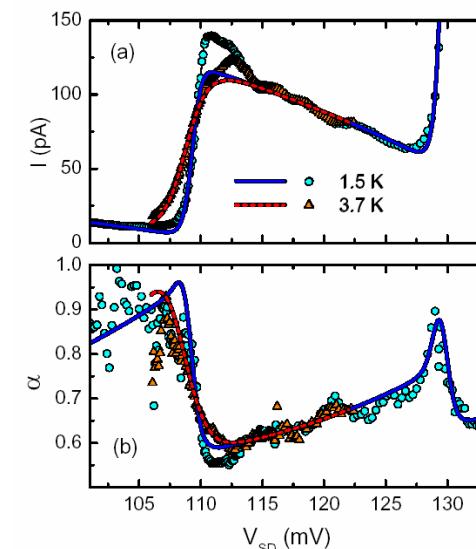
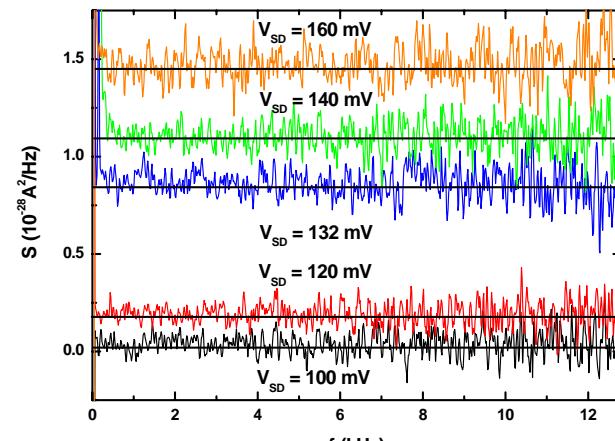
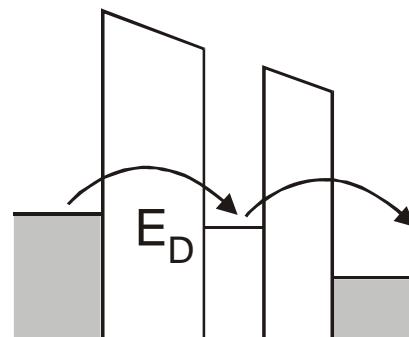
correlations can suppress noise

$$S = \alpha 2eI$$

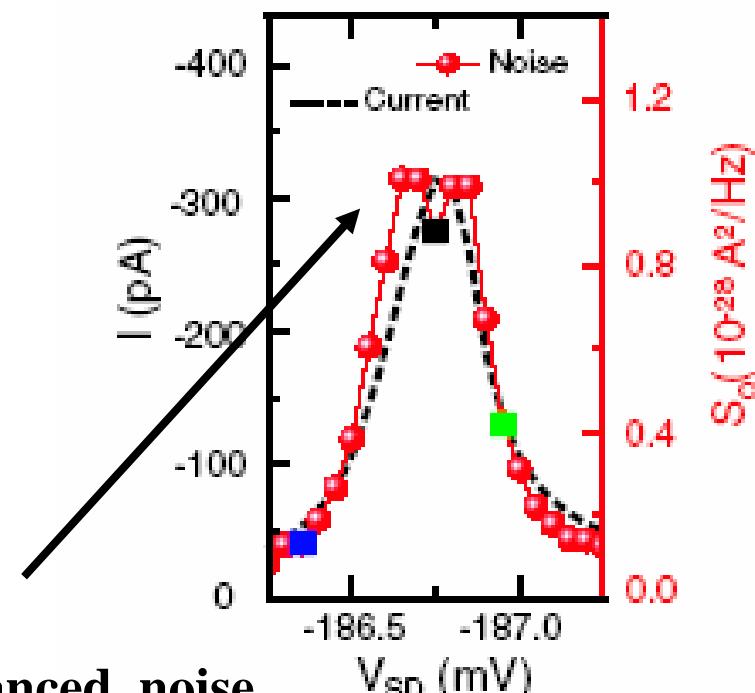
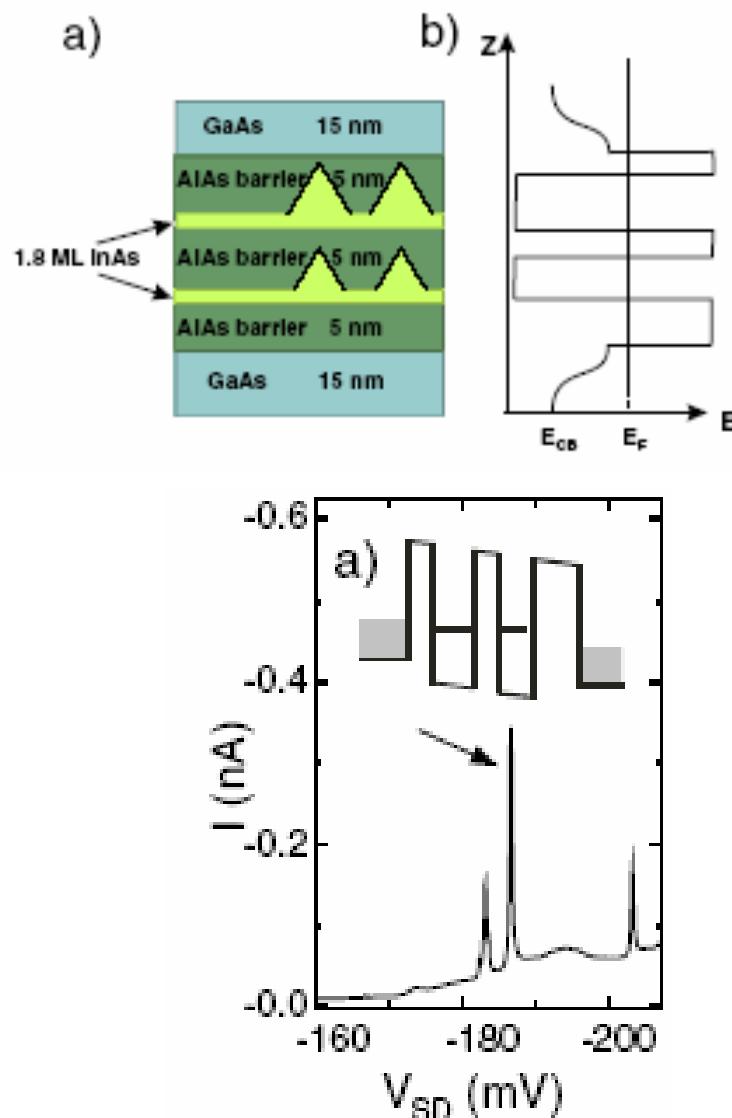
Fano factor

Phys. Rev. B 66, 161303 (2002)

Phys. Rev. B 69, 113316 (2004)



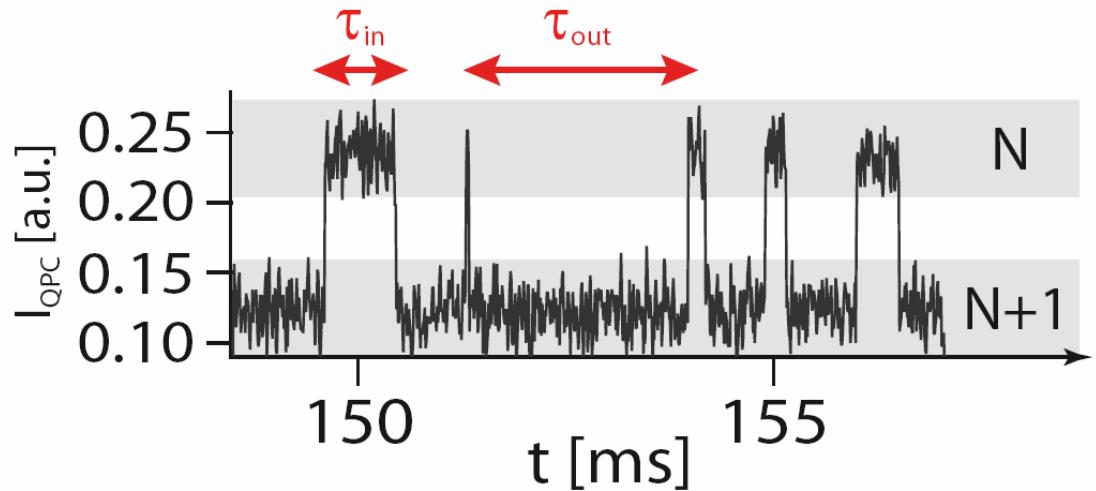
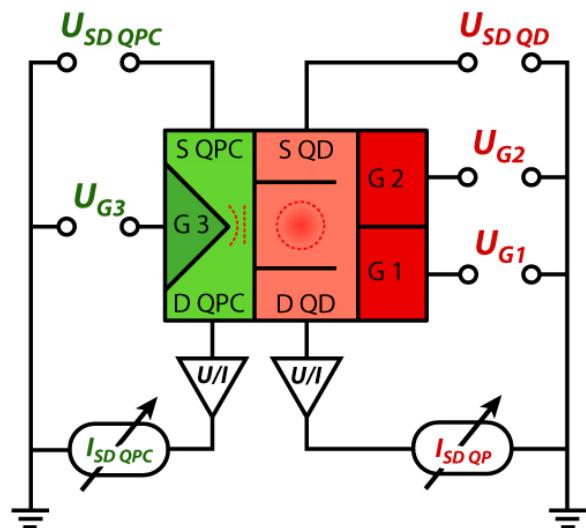
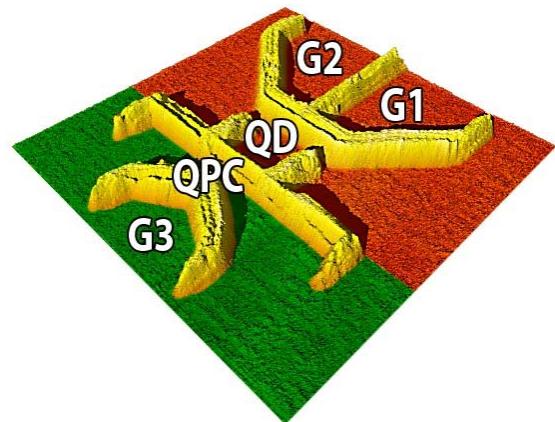
# Shot Noise in Coupled Quantum Dots



enhanced noise  
due to ??  
coupling effects, interactions, ...

Phys. Rev. Lett. 96, 246803 (2006)

# Real Time Detection of Single Electrons



direct analysis of tunneling properties

tunneling times, distribution,  
counting statistics  
Fano factor, ...

Phys. Rev. B 72, 193302 (2005)

Phys. Rev. B 72, 233402 (2005)



**N. Maire**



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**A. Hadzibrahimovic**



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**P. Barthold**



**M. Rogge**



**N. Ubbelohde**



**T. Ridder**



**Q. Ahmad**



**F. Luque**



**C. Fricke**



**A. Mühle**



**H. Schmidt**